



Overview & Applications

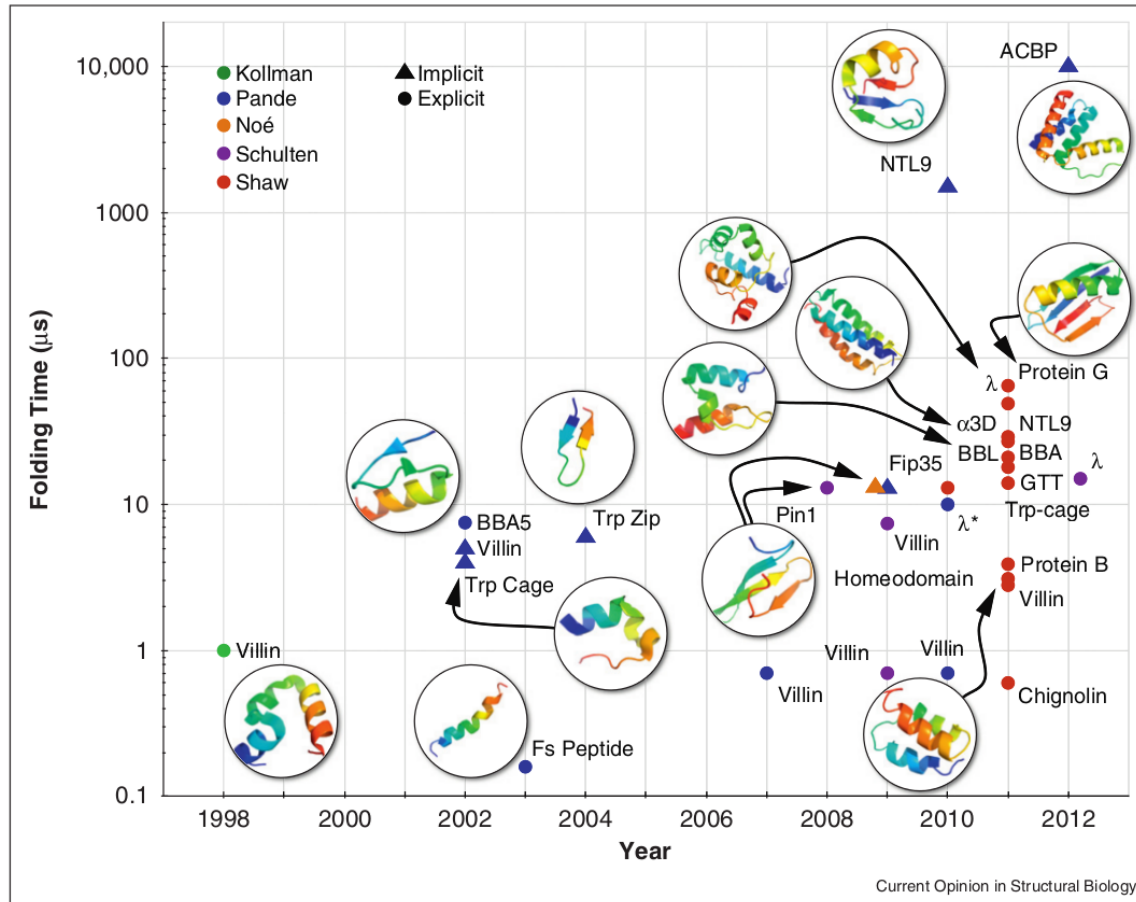
T. Lezon

Hands-on Workshop in Computational Biophysics

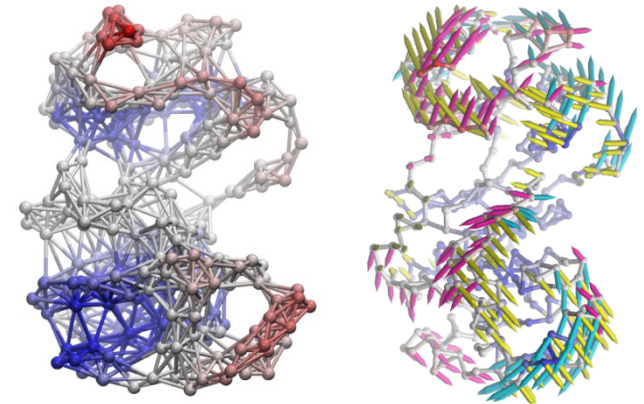
Pittsburgh Supercomputing Center

22 May, 2014

Simulations still take time



Lane et al. 2013



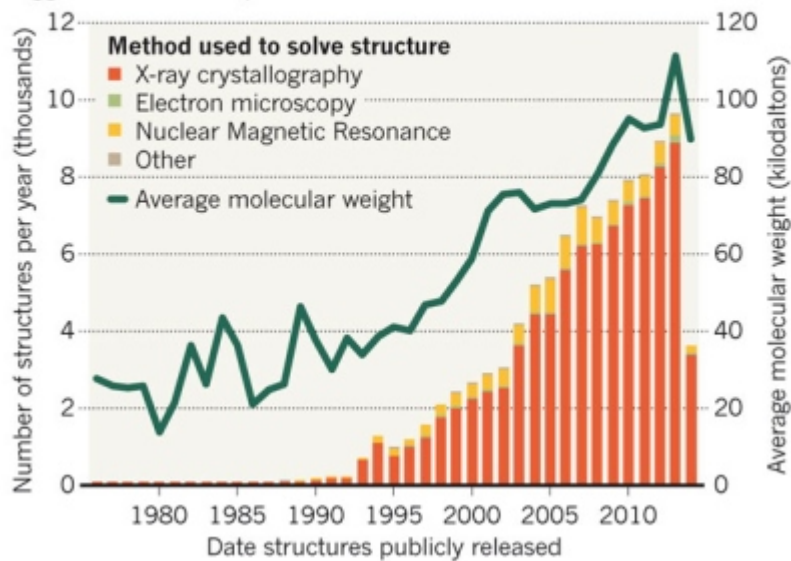
Bakan et al. Bioinformatics 2011.

Coarse-grained Elastic Network Models are fast

The structural data explosion

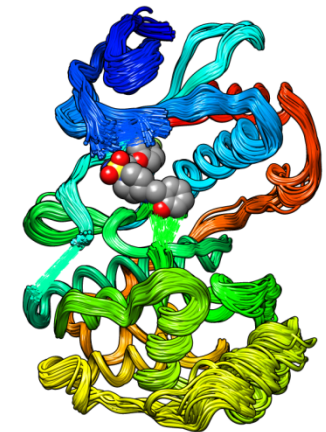
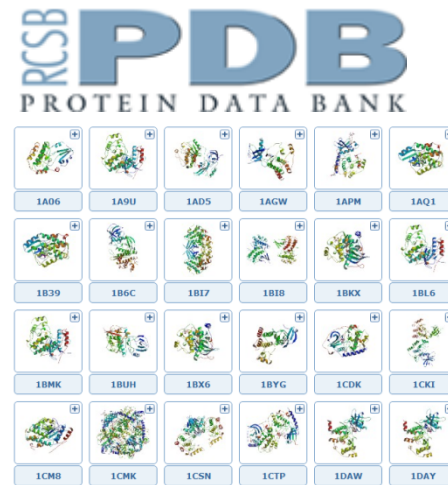
ONE HUNDRED THOUSAND PROTEIN STRUCTURES

Biomolecular structures stored in the Protein Data Bank are getting bigger and more complex.



Nature, 15 May 2014.

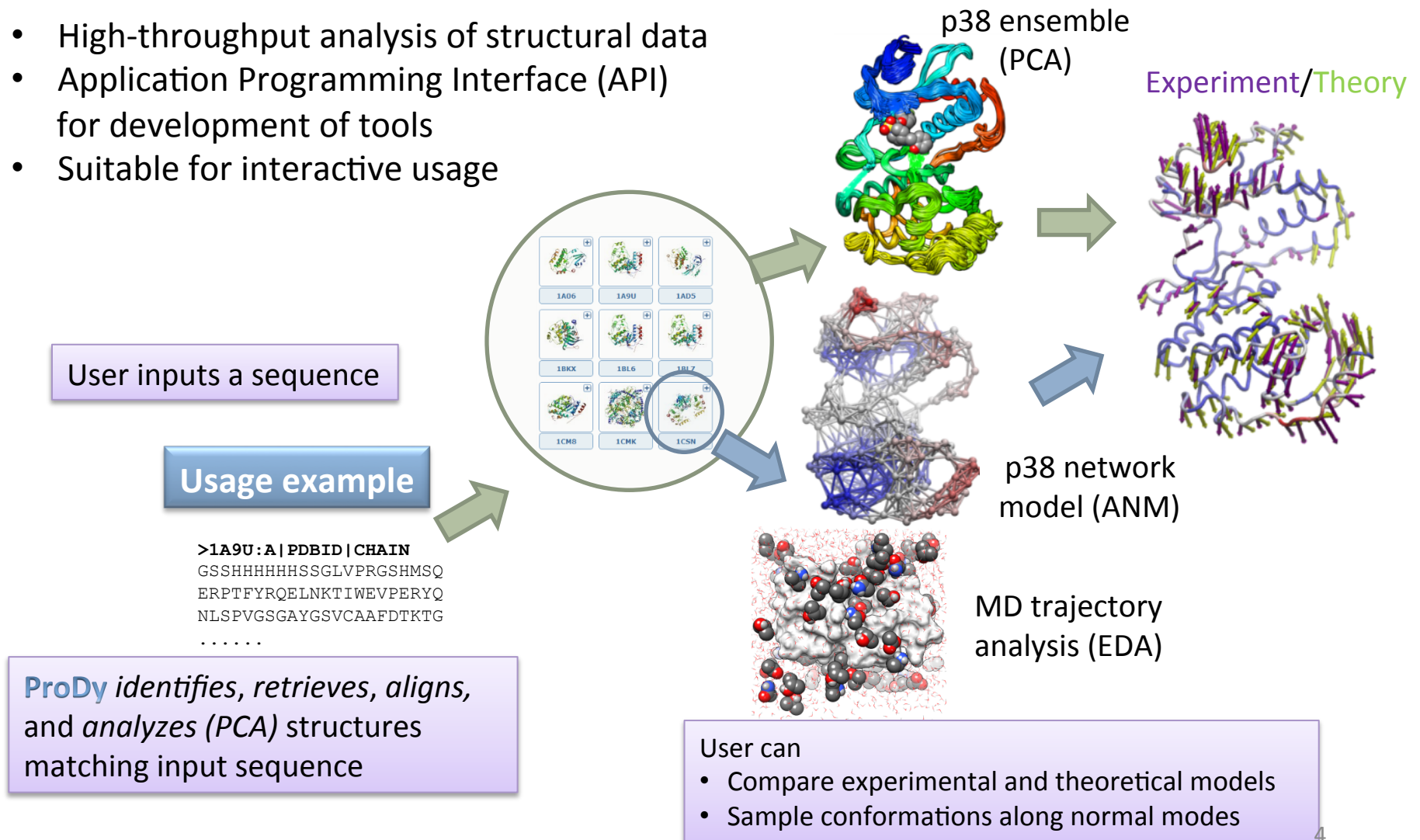
Multiple structures for a single sequence



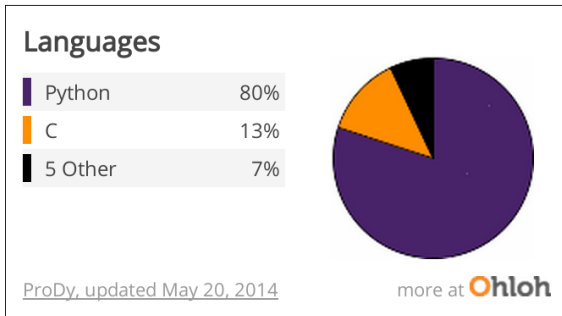
Dynamics may be inferred from structural data.

Exploiting the PDB since 2010

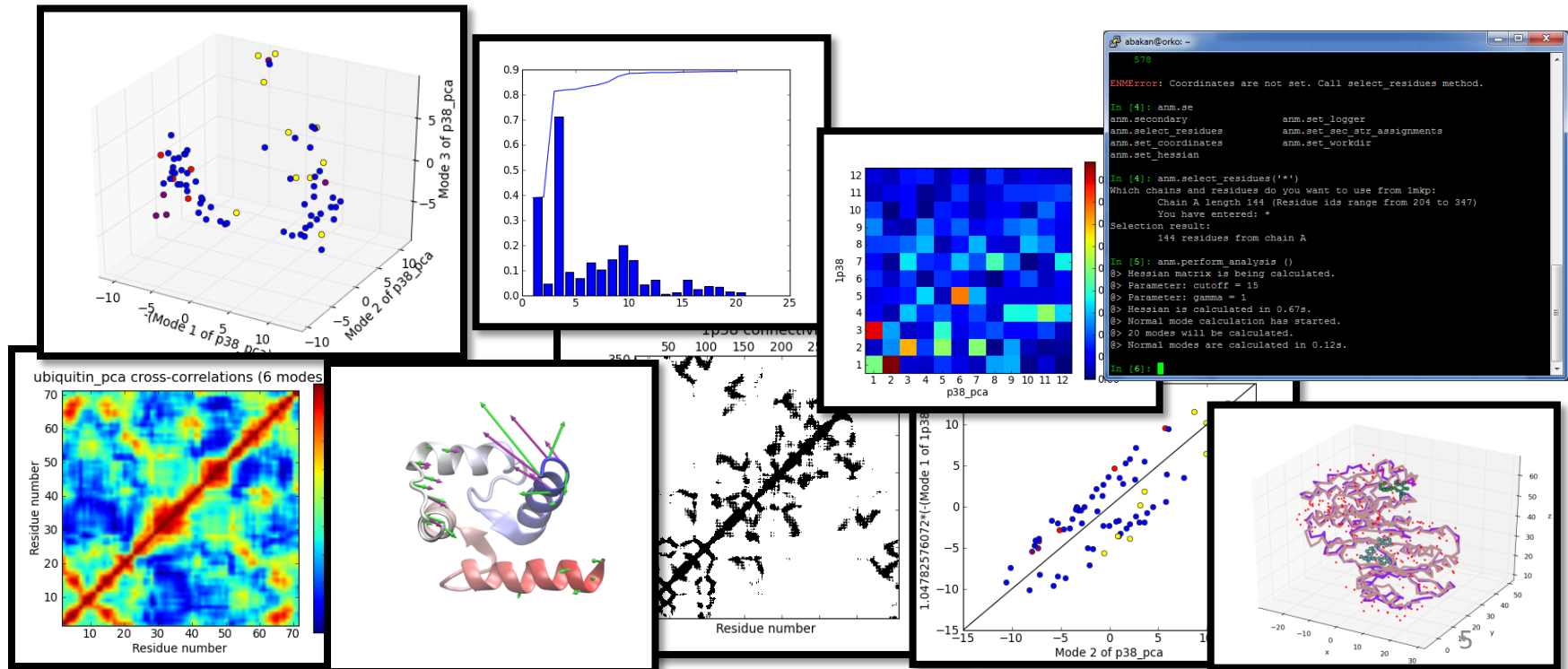
- High-throughput analysis of structural data
- Application Programming Interface (API) for development of tools
- Suitable for interactive usage



An Interactive Tool



IP[y]: IPython
Interactive Computing



An evolving suite of tools



Principal Component Analysis
Elastic Network Models
Normal Mode Analysis
Trajectory Analysis



Multiple Sequence Alignment
Correlated Mutation Analysis
Structural Evolution

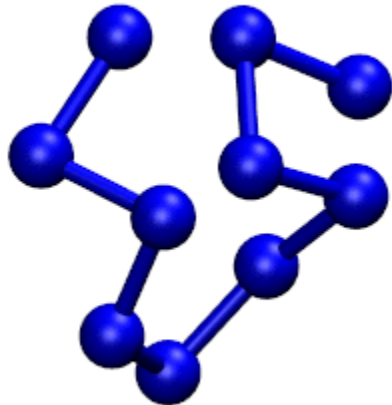


Computational Drug Discovery
Binding Site Prediction
Affinity Estimation



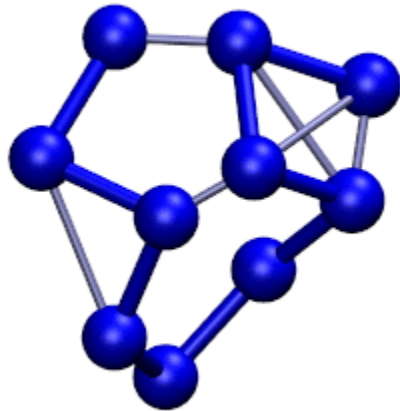
Call ProDy from VMD
Normal Mode Visualization

Elastic Network Model



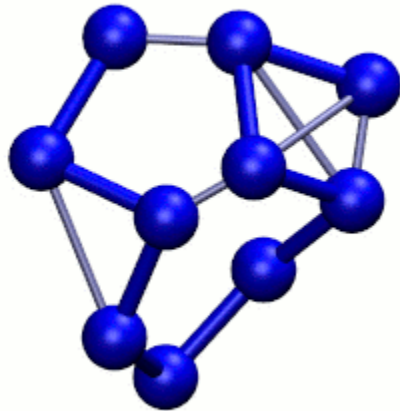
- Useful for finding global equilibrium motions of proteins
- Employs harmonic potential about native state
- Coarse-grained (C α -only description)
- Residue pairs are connected via springs
- Normal modes are found analytically

Elastic Network Model



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Elastic Network Model



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- Normal modes are found analytically

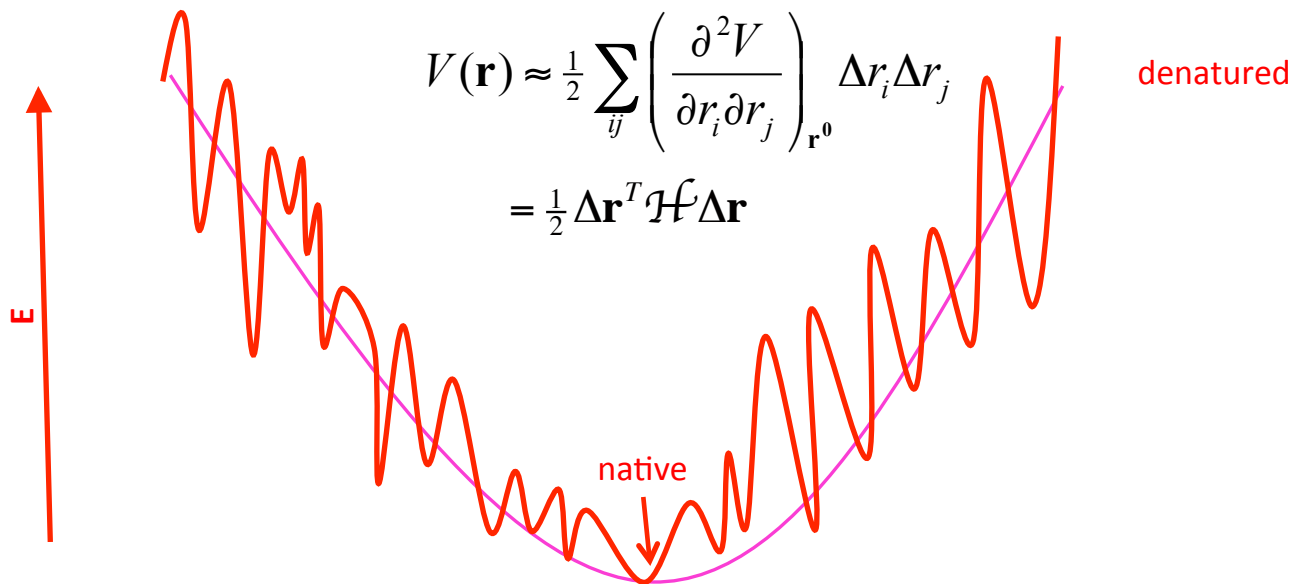
Approximating the protein free energy landscape

Rough and funnel-shaped energy landscape that is function of atomic coordinates

$$\mathbf{r} = (x_1, y_1, z_1, \dots, x_N, y_N, z_N)^T$$

$$\Delta \mathbf{r} = \mathbf{r} - \mathbf{r}^0$$

$$V(\mathbf{r}) = V(\mathbf{r}^0) + \sum_i \left(\frac{\partial V}{\partial r_i} \right)_{\mathbf{r}^0} \Delta r_i + \frac{1}{2} \sum_{ij} \left(\frac{\partial^2 V}{\partial r_i \partial r_j} \right)_{\mathbf{r}^0} \Delta r_i \Delta r_j + \frac{1}{6} \sum_{ijk} \left(\frac{\partial^3 V}{\partial r_i \partial r_j \partial r_k} \right)_{\mathbf{r}^0} \Delta r_i \Delta r_j \Delta r_k + \dots$$



Equations of Motion

$$\mathbf{M}\Delta\ddot{\mathbf{r}} = -\mathcal{H}\Delta\mathbf{r}$$

$$\begin{cases} \mathbf{q} = \mathbf{M}^{1/2}\Delta\mathbf{r} \\ \mathbf{H} = \mathbf{M}^{-1/2}\mathcal{H}\mathbf{M}^{-1/2} \end{cases}$$

Newton

Mass-weighted coordinates

Mass-weighted Hessian

$$\begin{aligned} \ddot{\mathbf{q}} &= -\mathbf{M}^{-1/2}\mathcal{H}\mathbf{M}^{-1/2}\mathbf{q} \\ &= -\mathbf{H}\mathbf{q} \end{aligned}$$

$$\begin{cases} \mathbf{q}(t) = \mathbf{q}e^{-i\omega t} \\ \ddot{\mathbf{q}}(t) = -\omega^2\mathbf{q}(t) \end{cases}$$

Oscillatory solution

$$\mathbf{H} = \mathbf{V}\mathbf{\Lambda}\tilde{\mathbf{V}}$$

$$\Lambda_{ij} = \omega_i^2 \delta_{ij}$$

Anisotropic Network Model

$$V(\mathbf{r}) = \frac{\gamma}{2} \sum_{i=1}^N \sum_{j>i} \underbrace{\left(|\mathbf{r}_{ij}| - |\mathbf{r}_{ij}^0| \right)^2}_{\text{Harmonic}} \underbrace{\Theta\left(R_c - |\mathbf{r}_{ij}^0| \right)}_{\text{Step function}}$$

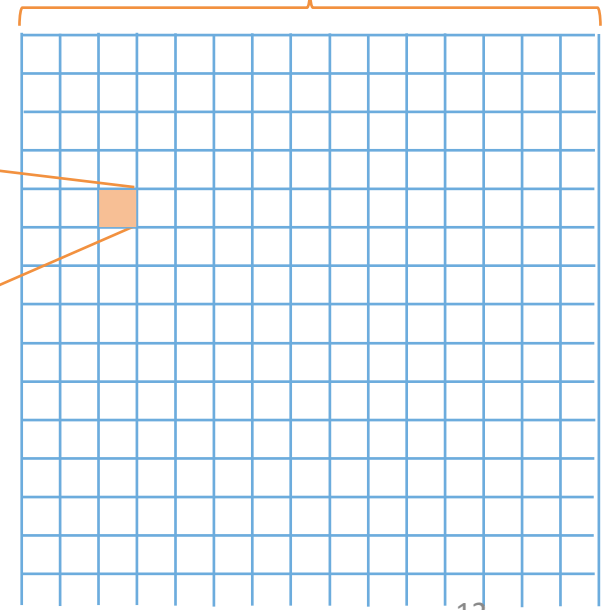
Harmonic Step function

$$\left(\frac{\partial^2 V}{\partial x_i \partial y_j} \right)_{\mathbf{r}^0} = - \frac{x_i^0 y_j^0}{|\mathbf{r}_{ij}^0|^2}$$

Hessian is calculated
directly from structure

3N

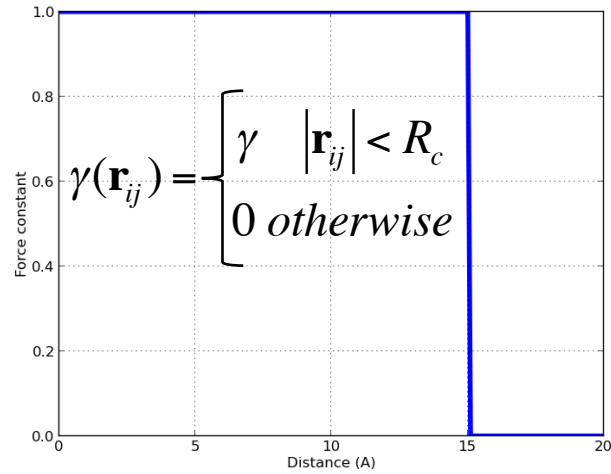
$$\mathbf{H}_{ij} = - \frac{\gamma}{(R_{ij}^0)^2} \begin{bmatrix} (x_{ij}^0)^2 & x_{ij}^0 y_{ij}^0 & x_{ij}^0 z_{ij}^0 \\ x_{ij}^0 y_{ij}^0 & (y_{ij}^0)^2 & y_{ij}^0 z_{ij}^0 \\ x_{ij}^0 z_{ij}^0 & y_{ij}^0 z_{ij}^0 & (z_{ij}^0)^2 \end{bmatrix}$$



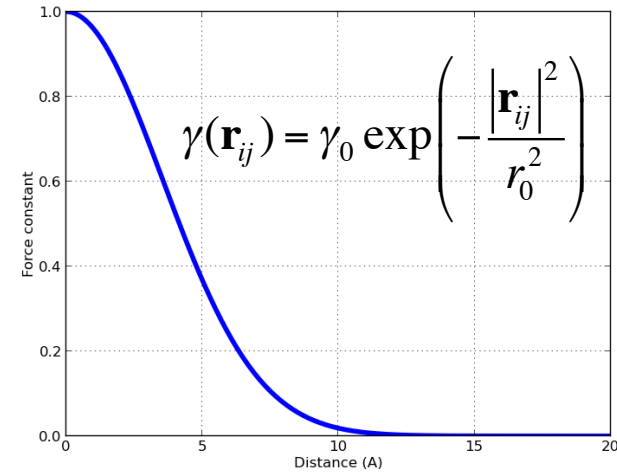
ENMs are flexible!

- Selection of the ENM force constants
 - Cutoff distance
 - Functional form
- Changing the potential directly
- Adding rigidity
- Including external elements, or looking at only a subsystem
- Altering network topology

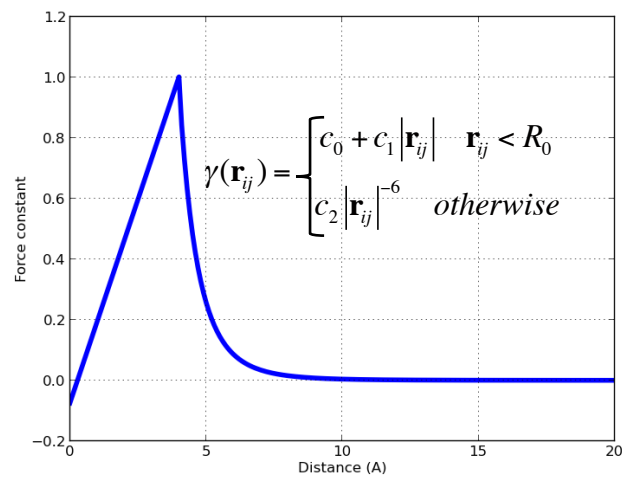
Flexible force constants



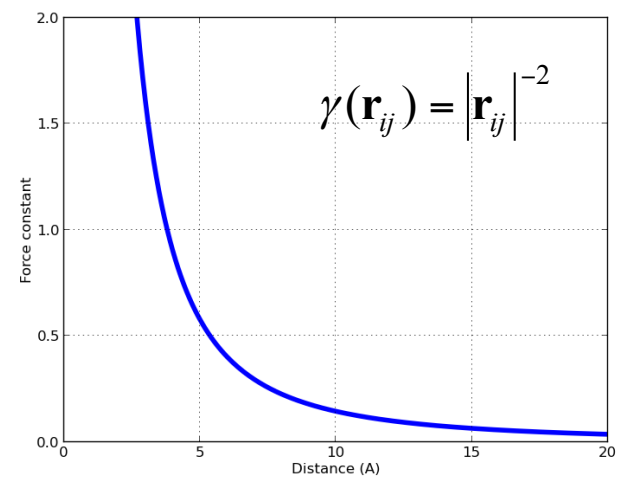
Tirion, PRL 77 (1996).



Hinsen et al. Proteins 33 (1998).



Hinsen et al. Chem Phys 261 (2000).



Yang et al. PNAS 106 (2009).

Optimizing force constants

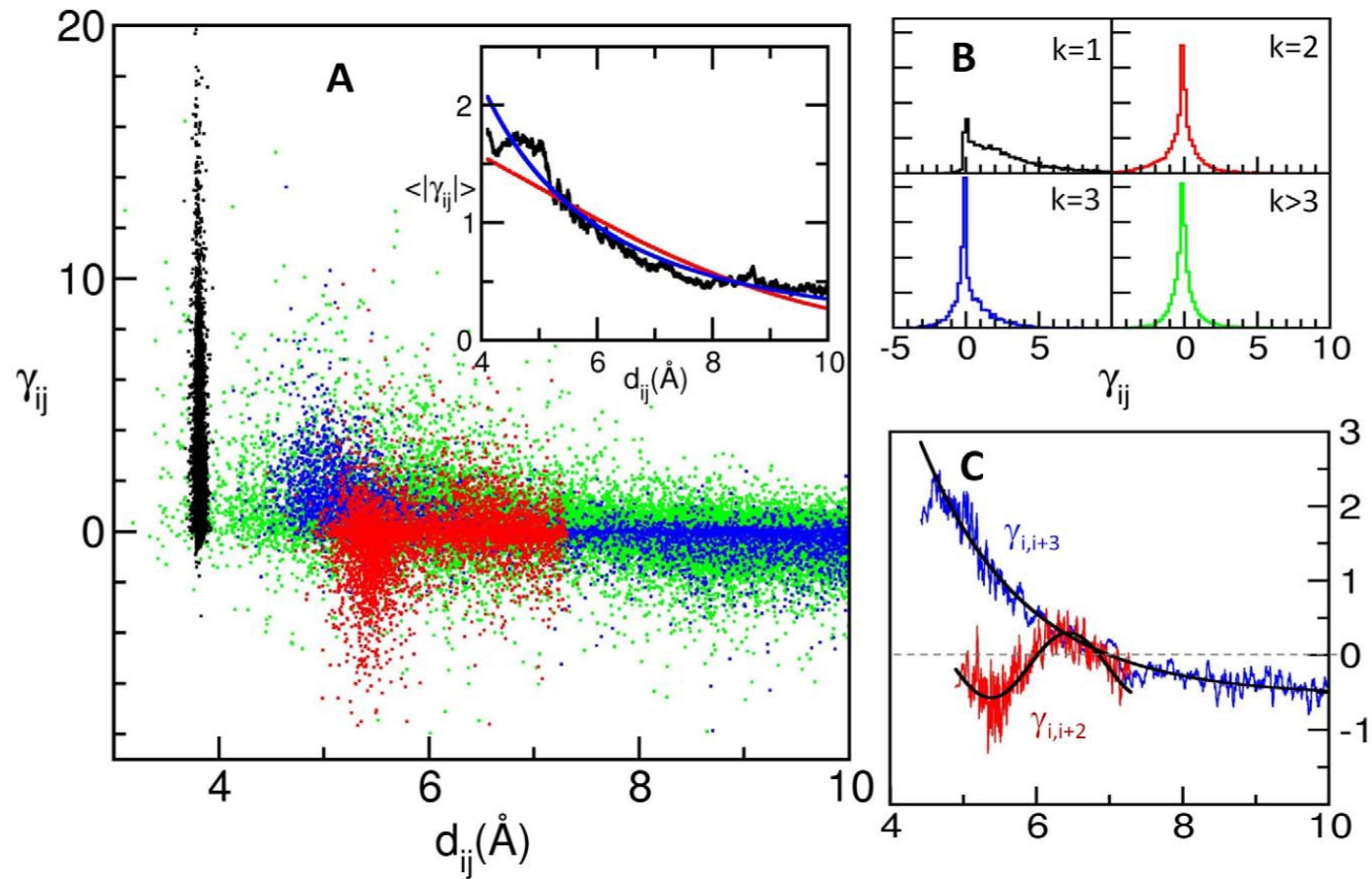
- Download NMR structures from PDB
- Calculate residue MSFs for each protein
- Assign ENM topology
- Optimize force constants to reproduce structural dynamics
- Search for trends in force constant values with structure

fetchPDB()

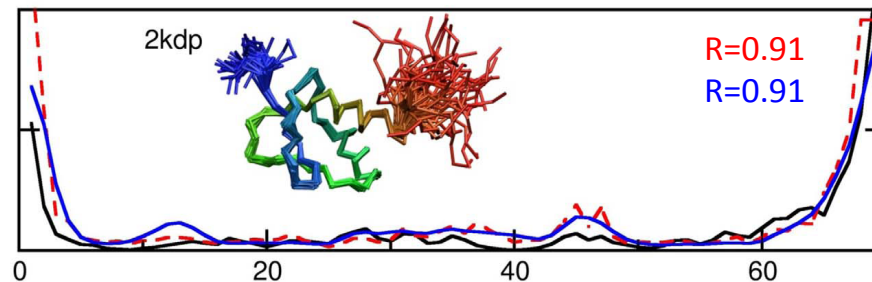
calcMSF()

buildHessian()

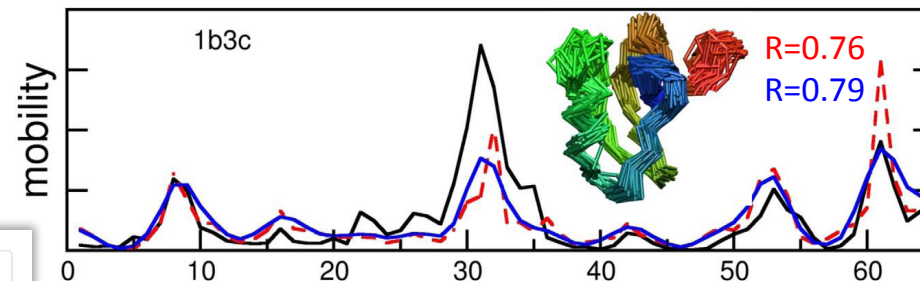
Flexible force constants



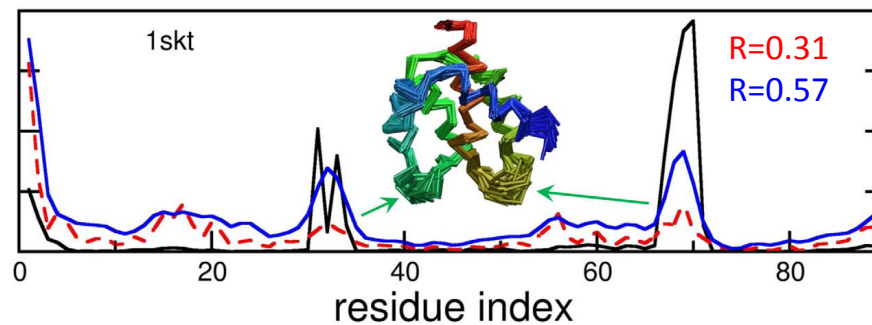
Fine-tuning force constants



- Distance-dependence
- 1st neighbors
- 2nd neighbors
- H bonds



black: NMR
red: ENM
blue: modified ENM



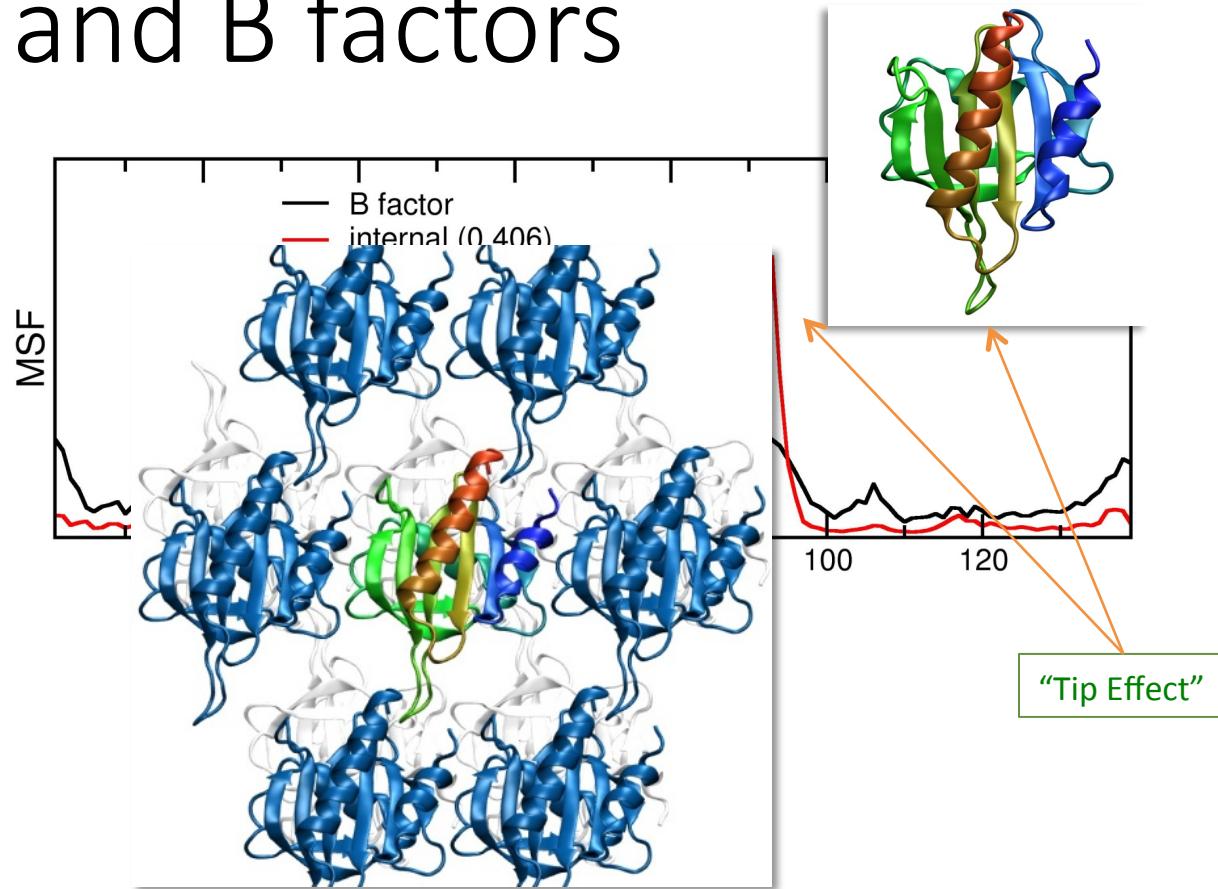
GammaStructureBased()

Elastic Network Models

Learn how to perform normal mode analysis and developing customized force constant functions.

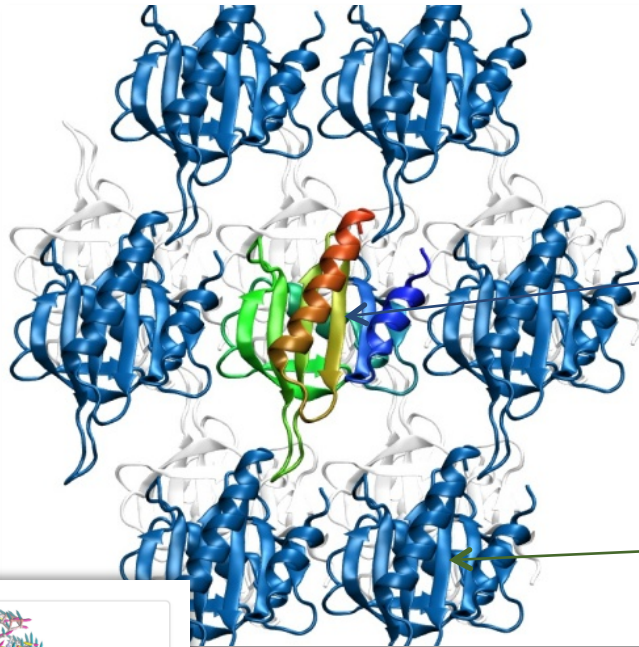
[Go to Tutorial](#)

Improving correlation between ENM and B factors

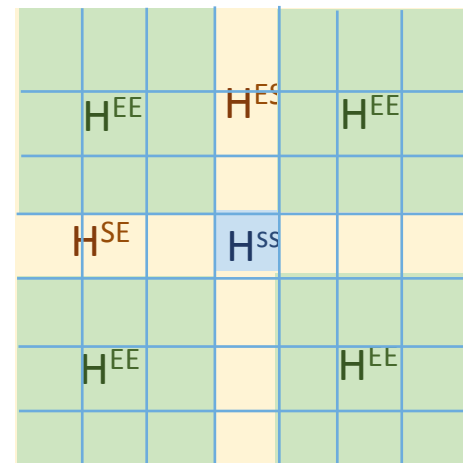


Possible solution: Add crystal contacts

Explicit membrane models



“system”




“environment”

As the *environment* fluctuates randomly, the effective motion of the *system* is given by

$$V_{eff}(\mathbf{s}) = \frac{1}{2} \Delta \mathbf{s}^T (\mathbf{H}^{ss'}) \Delta \mathbf{s}$$

$$\mathbf{H}^{ss'} = \mathbf{H}^{ss} - \mathbf{H}^{SE} (\mathbf{H}^{EE})^{-1} \mathbf{H}^{ES}$$

reduceModel()

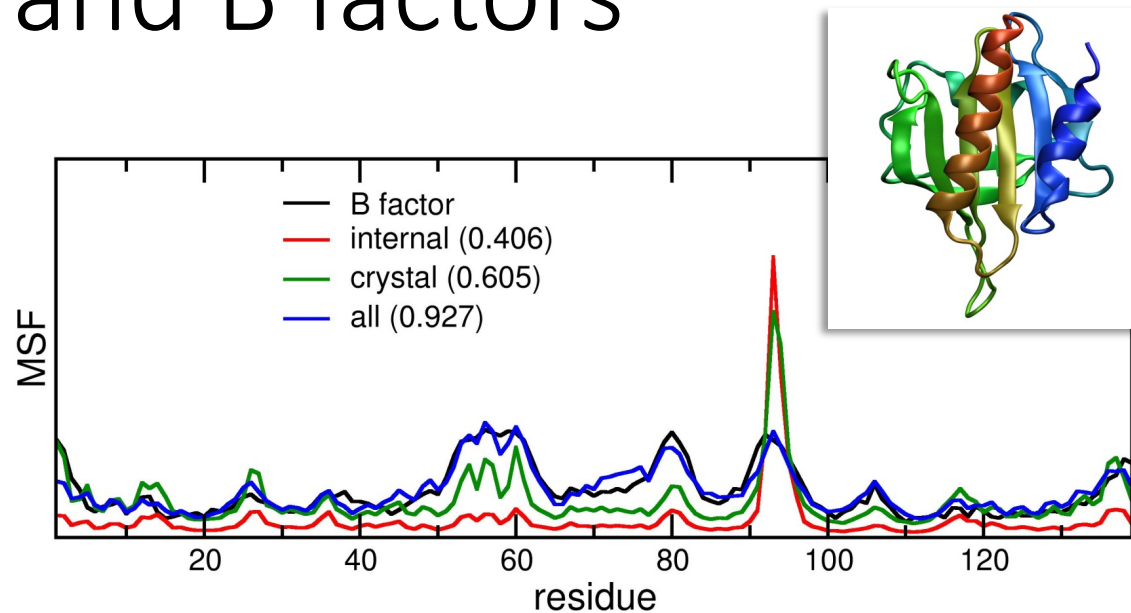


Elastic Network Models

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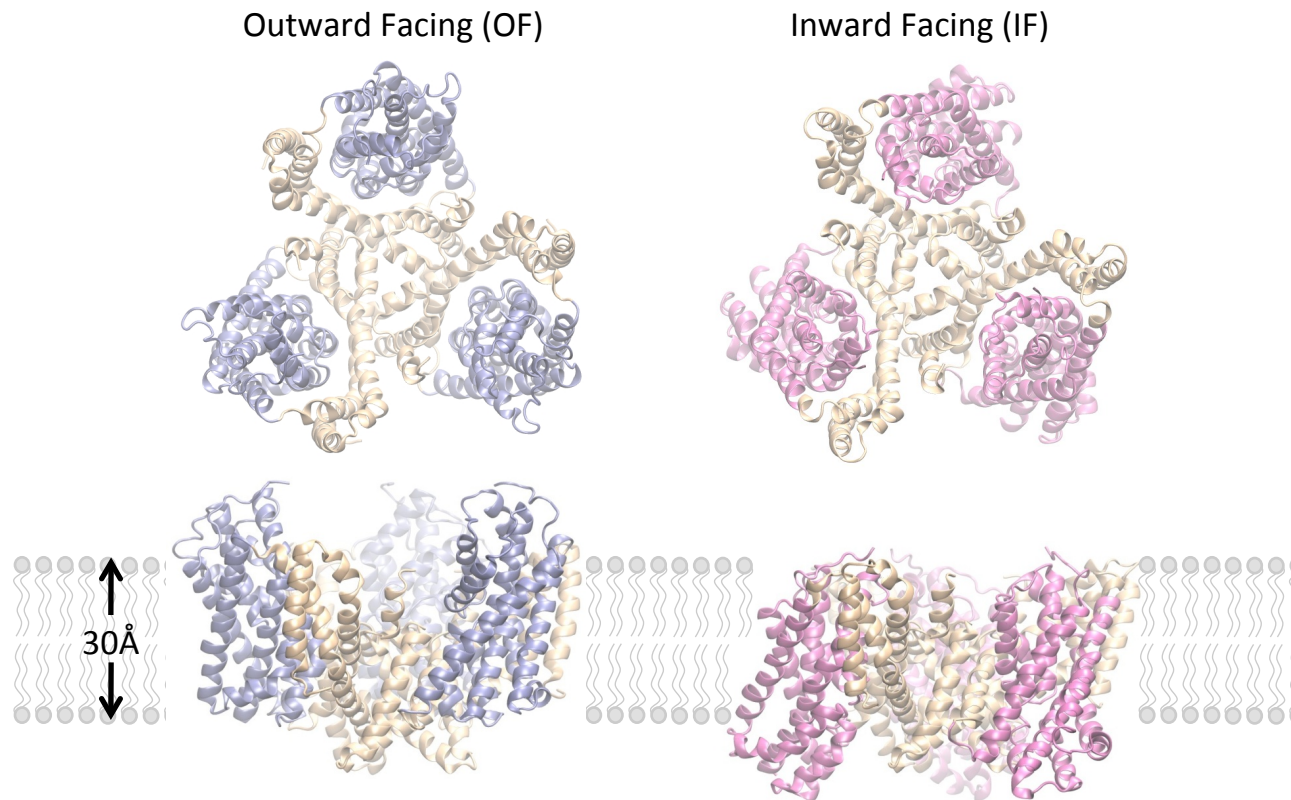
[Go to Tutorial](#)

Improving correlation between ENM and B factors



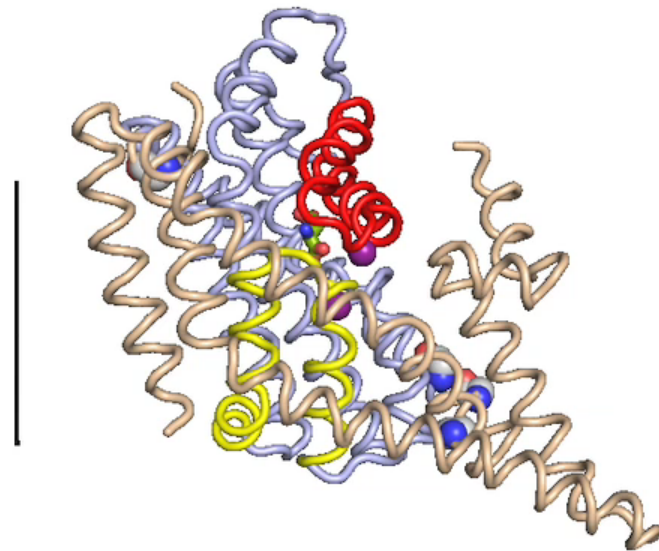
Crystal contacts help, but do not eliminate tip effect.
What about lattice vibrations?

Global transitions

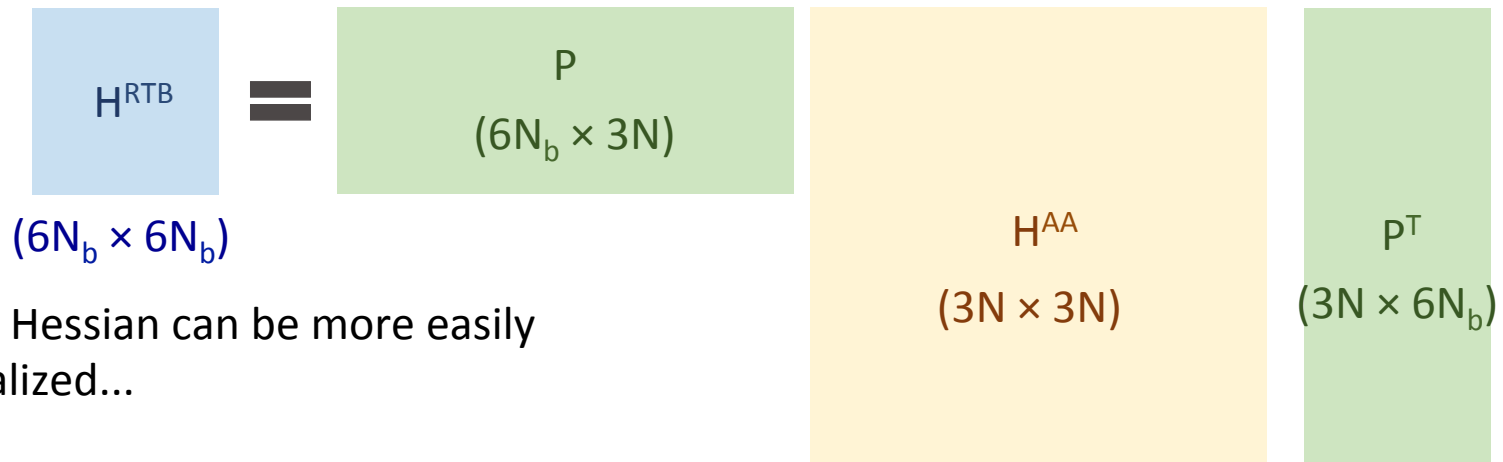


Global transitions

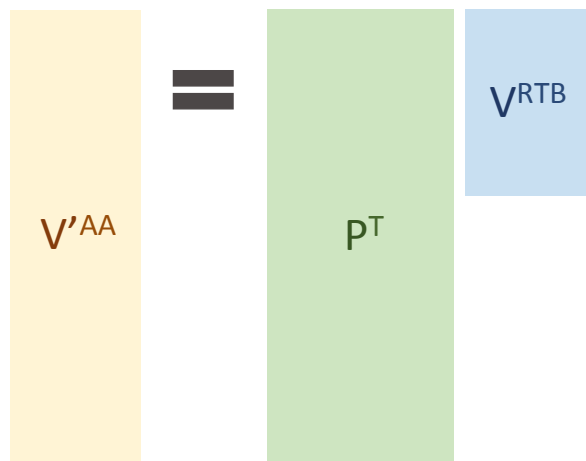
Single subunit showing the
transport domain moving
across the membrane



Rotations-Translations of Blocks



Smaller Hessian can be more easily diagonalized...



- H: ANM Hessian (3 rows/cols per residue)
- P: Projection matrix from all-residue space to rigid block space
- H^{RTB} : RTB Hessian (no internal motions of blocks)
- V^{AA} : Approximate ANM motions
- `RTB.buildHessian()`

...and modes projected back into all-residue space

Ming & Wall. PRL 95 (2005).
 Zheng & Brooks. Biophys J 89 (2005).

Exploring structural transitions: Glutamate transporter

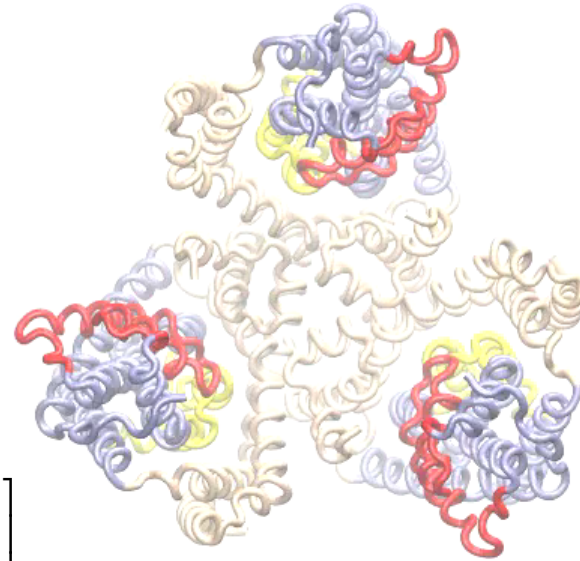
ANM predicts large radial motions of the trimer. Can we invent a better model?

$$\mathbf{H}_{ij} = -\frac{\gamma}{(R_{ij}^0)^2} \begin{bmatrix} (x_{ij}^0)^2 & x_{ij}^0 y_{ij}^0 & x_{ij}^0 z_{ij}^0 \\ x_{ij}^0 y_{ij}^0 & (y_{ij}^0)^2 & y_{ij}^0 z_{ij}^0 \\ x_{ij}^0 z_{ij}^0 & y_{ij}^0 z_{ij}^0 & (z_{ij}^0)^2 \end{bmatrix}$$

Altered radial force constants:

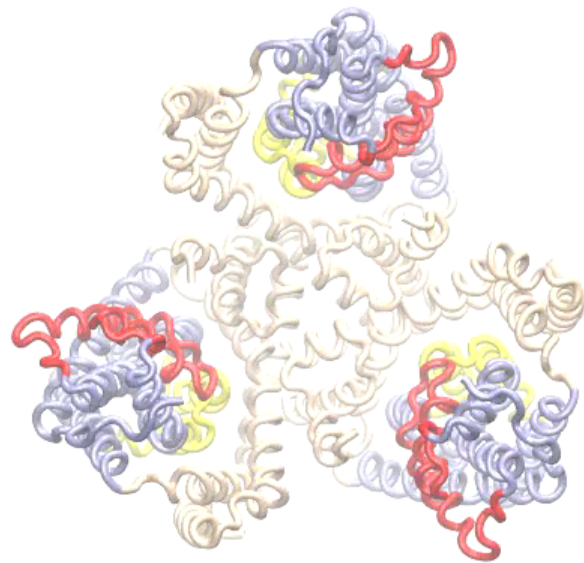
$$\mathbf{H}_{ij} = -(R_{ij}^0)^{-2} \begin{bmatrix} (x_{ij}^0 \sqrt{\gamma_x})^2 & x_{ij}^0 y_{ij}^0 \sqrt{\gamma_x \gamma_y} & x_{ij}^0 z_{ij}^0 \sqrt{\gamma_x \gamma_z} \\ x_{ij}^0 y_{ij}^0 \sqrt{\gamma_x \gamma_y} & (y_{ij}^0 \sqrt{\gamma_y})^2 & y_{ij}^0 z_{ij}^0 \sqrt{\gamma_y \gamma_z} \\ x_{ij}^0 z_{ij}^0 \sqrt{\gamma_x \gamma_z} & y_{ij}^0 z_{ij}^0 \sqrt{\gamma_y \gamma_z} & (z_{ij}^0 \sqrt{\gamma_z})^2 \end{bmatrix}$$

$$\mathbf{H}_{ij} = -\frac{\gamma}{(R_{ij}^0)^2} \begin{bmatrix} (x_{ij}^0)^2 & x_{ij}^0 y_{ij}^0 & cx_{ij}^0 z_{ij}^0 \\ x_{ij}^0 y_{ij}^0 & (y_{ij}^0)^2 & cy_{ij}^0 z_{ij}^0 \\ cx_{ij}^0 z_{ij}^0 & cy_{ij}^0 z_{ij}^0 & (cz_{ij}^0)^2 \end{bmatrix}$$

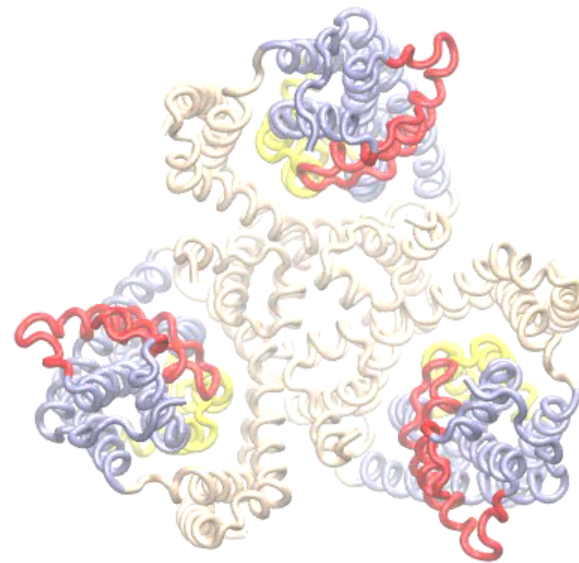


RTB.buildHessian()

Exploring structural transitions: Glutamate transporter

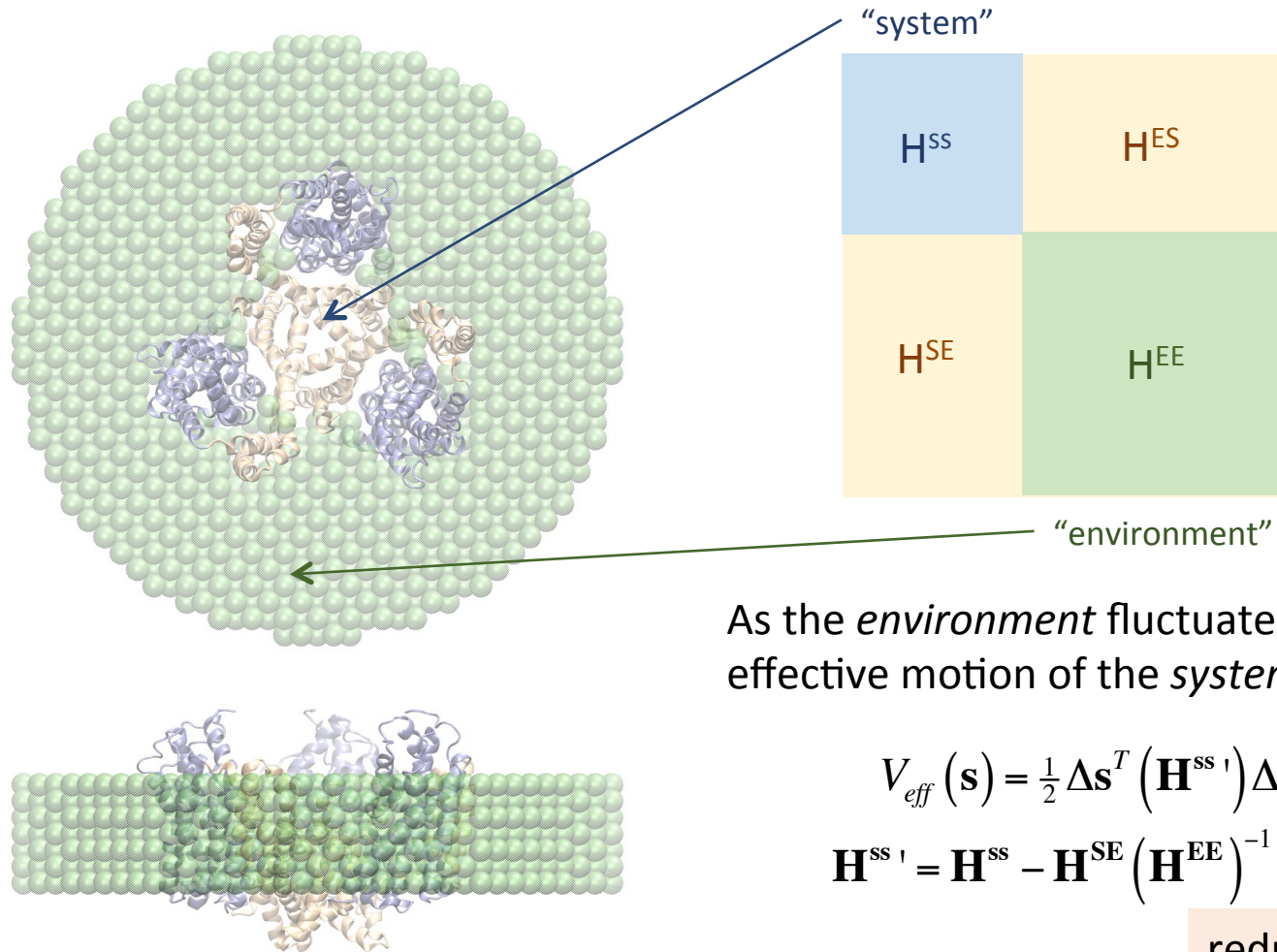


ANM: Large radial motions

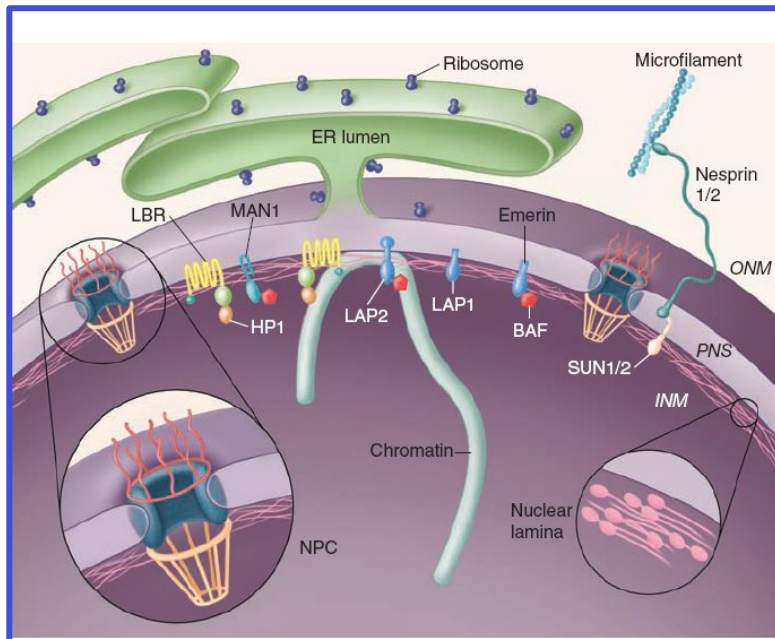


imANM

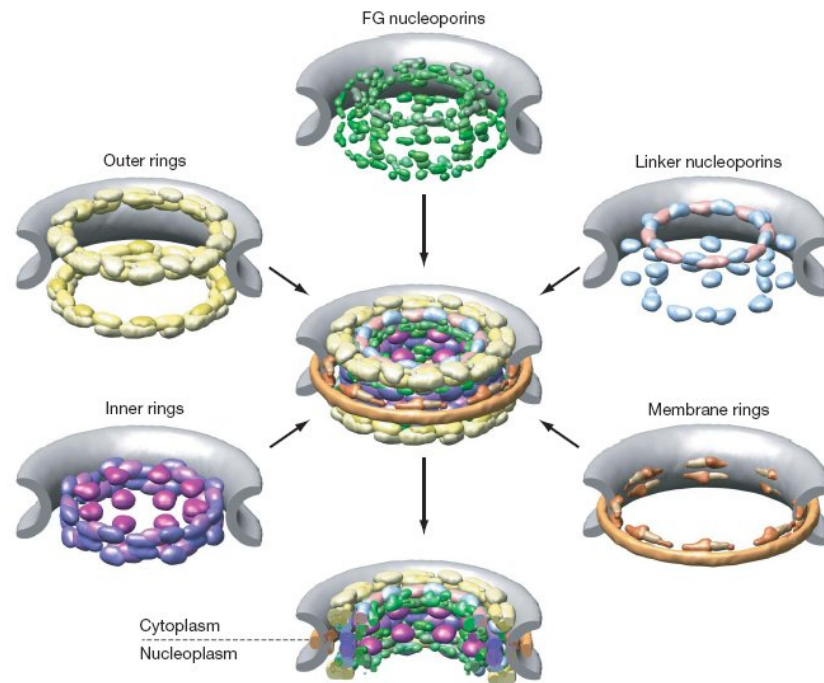
Explicit membrane models



Thinking bigger: NPC



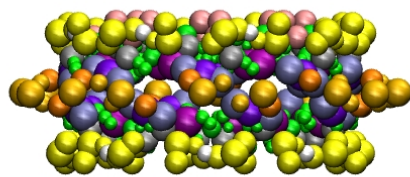
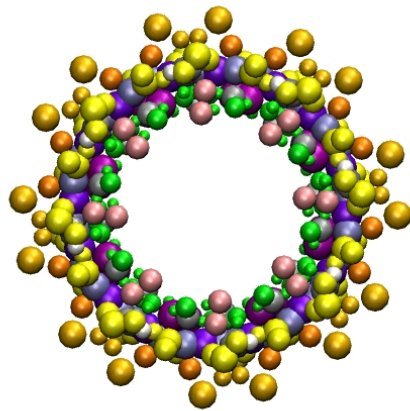
Stewart *et al.* Science 318 (2007).



Alber *et al.* Nature 450 (2007).

ENM of NPC

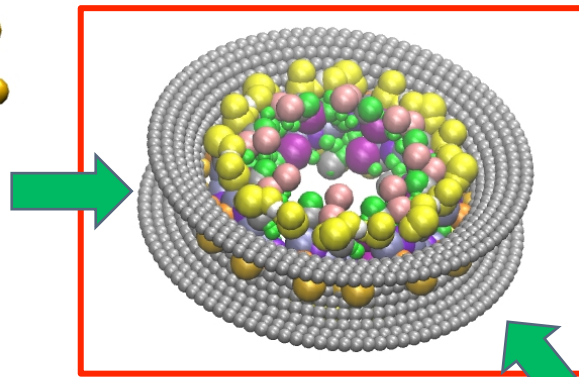
NPC Model



456 proteins:
57 proteins/spoke
30 unique proteins

$$R_c = \begin{cases} 12\text{nm protein-protein} \\ 8\text{nm NE-NE} \\ 10\text{nm protein-NE} \end{cases}$$

$$\gamma = \begin{cases} 1.0 \text{ protein-protein} \\ 10 \text{ NE-NE} \end{cases}$$

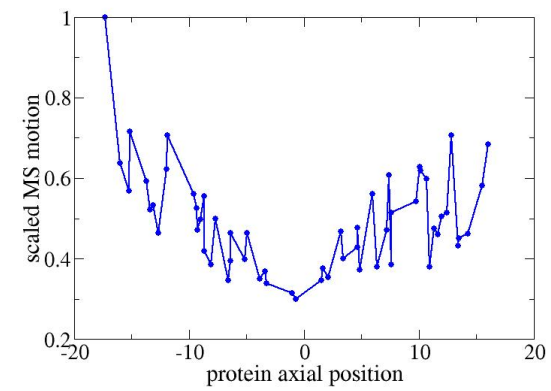
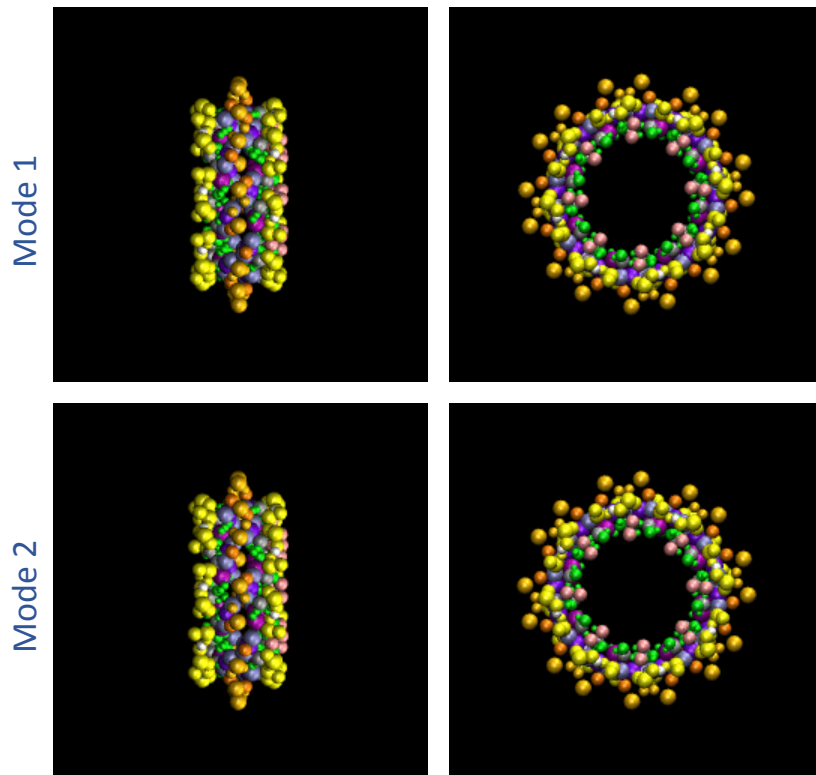


NE:
2070 discrete points



gammaVariableCutoff()
reduceModel()
parseSparseMatrix()

NPC slow modes

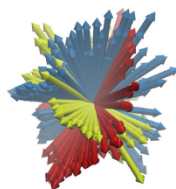


Tutorials



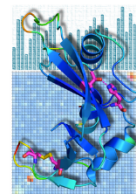
ProDy

Learn how to use ProDy from the introductory ProDy tutorial or from the comprehensive API reference manual.



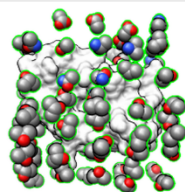
Normal Mode Wizard

Learn how to depict normal modes and generate animations of protein dynamics along them with NMWiz.



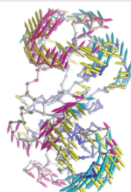
Evol

Learn how to identify conserved and coevolved residues and characterizing their dynamical properties.



Drugability Suite

Learn how to setup and analyze druggability simulations containing small organic molecules using DruGUI.



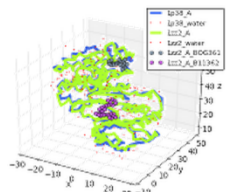
Elastic Network Models

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Ensemble Analysis

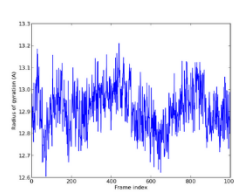
Learn how to analyze large and heterogeneous ensembles of protein structures to infer dynamical properties.



Structure Analysis

Learn how to compare and align structures, identify ligand contacts, and extract ligands from PDB files.

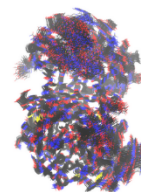
[Go to Tutorial](#)



Trajectory Analysis

Learn how to analyze simulation trajectories, in particular handling large trajectory files that don't fit in memory.

[Go to Tutorial](#)



Conformational Sampling

Learn how to generate alternate protein conformations along ANM modes and to refine them using NAMD.

[Go to Tutorial](#)